Advanced Lectures in Mathematics Volume 44

Proceedings of the Seventh International Congress of Chinese Mathematicians

Volume II

Companion to the volume Proceedings of the Seventh International Congress of Chinese Mathematicians, *Volume I*

edited by

Lizhen Ji \cdot Lo Yang \cdot Shing-Tung Yau





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Editors:

Lizhen Ji (Department of Mathematics, University of Michigan) Lo Yang (Institute of Mathematics, Chinese Academy of Sciences) Shing-Tung Yau (Department of Mathematics, Harvard University)

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ADVANCED LECTURES IN MATHEMATICS

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The scene of opening ceremony



Prof. Shing-Tung Yau gave opening speech



Left to right: Prof. Shing-Tung Yau, Prof. Björn Engquist (the awardee of the International Cooperation Award), and Prof. Zhong-Ci Shi



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Prof. Edward Witten and Prof. Shing-Tung Yau



Left to right: Prof. Shing-Tung Yau, Prof. Yuefei Wang, Prof. Chunli Bai (President of CAS), and Prof. Yong Qiu (President of Tsinghua University)

Preface

Every three years, mathematicians of Chinese descent meet for five days to present their results on mathematics and related subjects. Traditionally, the first day of the meeting is organized by the Morningside Foundation, where the prestigious Morningside Awards, the Chern Award, and the International Cooperation Awards are given. In 2016, the International Congress of Chinese mathematicians (ICCM) was organized by the Morningside Center of Mathematics in cooperation with the Academy of Mathematics and Systems Science at Chinese Academy of Sciences. The ceremony was held in the Great Hall of the People in China. Nearly two thousand Chinese mathematicians from all over the world came to Beijing for this ceremony. Many outstanding mathematicians of non-Chinese descent also came and gave spectacular lectures. We are glad that a large number of speakers have been willing to write up their lectures, and we have finally collected these manuscriptsthrough the hard work of Guangqiang Tie, and others. These papers provide good insight into the current status of many subjects in mathematics. We are proud to present them collected here. We should like to thank all participants, and the Morningside Center of Mathematics, for making such an effort to make the ICCM meeting and the publication of its proceedings successful.

Lizhen Ji, Lo Yang and Shing-Tung Yau

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