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# Advanced Lectures in Mathematics Volume 37

# Proceedings of the Sixth International Congress of Chinese Mathematicians

## Volume II

Companion to the volume Proceedings of the Sixth International Congress of Chinese Mathematicians, *Volume I* 

edited by

Chang-Shou Lin · Lo Yang Shing-Tung Yau · Jing Yu





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#### **Editors**

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