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Volume XXV

Handbook of Moduli

Volume II

edited by

Gavril Farkas · Ian Morrison

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The Handbook of Moduli *is dedicated to the memory of Eckart Viehweg, whose untimely death precluded a planned contribution, and to David Mumford, who first proposed the project, for all that they both did to nurture its subject; and to Angela Ortega and Jane Reynolds for everything that they do to sustain its editors.*

Contents

Volume I

Preface
Gavril Farkas and Ian Morrison xiii

Logarithmic geometry and moduli
Dan Abramovich, Qile Chen, Danny Gillam, Yuhao Huang, Martin Olsson, Matthew Satriano and Shenghao Sun 1

Invariant Hilbert schemes
Michel Brion 63

Algebraic and tropical curves: comparing their moduli spaces
Lucia Caporaso 119

A superficial working guide to deformations and moduli
F. Catanese 161

Moduli spaces of hyperbolic surfaces and their Weil–Petersson volumes
Norman Do 217

Equivariant geometry and the cohomology of the moduli space of curves
Dan Edidin 259

Tautological and non-tautological cohomology of the moduli space of curves
C. Faber and R. Pandharipande 293

Alternate compactifications of moduli spaces of curves
Maksym Fedorchuk and David Ishii Smyth 331

The cohomology of the moduli space of Abelian varieties
Gerard van der Geer 415

Moduli of K3 surfaces and irreducible symplectic manifolds
V. Gritsenko, K. Hulek and G.K. Sankaran 459

Normal functions and the geometry of moduli spaces of curves
Richard Hain 527

Volume II

Parameter spaces of curves
Joe Harris 1

Global topology of the Hitchin system
Tamás Hausel 29

Differential forms on singular spaces, the minimal model program, and hyperbolicity of moduli stacks
Stefan Kebekus 71

Contractible extremal rays on $\overline{M}_{0,n}$
Seán Keel and James M^{c}Kernan 115

Moduli of varieties of general type
János Kollár 131

Singularities of stable varieties
Sándor J Kovács 159

Soliton equations and the Riemann-Schottky problem
I. Krichever and T. Shiota 205

GIT and moduli with a twist
Radu Laza 259

Good degenerations of moduli spaces
Jun Li 299

Localization in Gromov-Witten theory and Orbifold Gromov-Witten theory
Chiu-Chu Melissa Liu 353

From WZW models to modular functors
Eduard Looijenga 427

Shimura varieties and moduli
J.S. Milne 467

The Torelli locus and special subvarieties
Ben Moonen and Frans Oort 549

Volume III

Birational geometry for nilpotent orbits
Yoshinori Namikawa 1

Cell decompositions of moduli space, lattice points and Hurwitz problems
Paul Norbury 39

Moduli of abelian varieties in mixed and in positive characteristic
Frans Oort 75

Local models of Shimura varieties, I. Geometry and combinatorics
Georgios Pappas, Michael Rapoport and Brian Smithling 135

Generalized theta linear series on moduli spaces of vector bundles on curves
Mihnea Popa 219

Computer aided unirationality proofs of moduli spaces
Frank-Olaf Schreyer 257

Deformation theory from the point of view of fibered categories
Mattia Talpo and Angelo Vistoli 281

Mumford's conjecture — a topological outlook
Ulrike Tillmann 399

Rational parametrizations of moduli spaces of curves
Alessandro Verra 431

Hodge loci
Claire Voisin 507

Homological stability for mapping class groups of surfaces
Nathalie Wahl 547