

Group Analysis of fMRI Data Using  $L_1$  and  $L_2$   
Regularization – Supplement

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Figure 1: Three randomly selected simulation runs with  $m = 10$  and no random effects, using L1 (red) and L2 (blue) regularization and AIC. The true curves are in black.

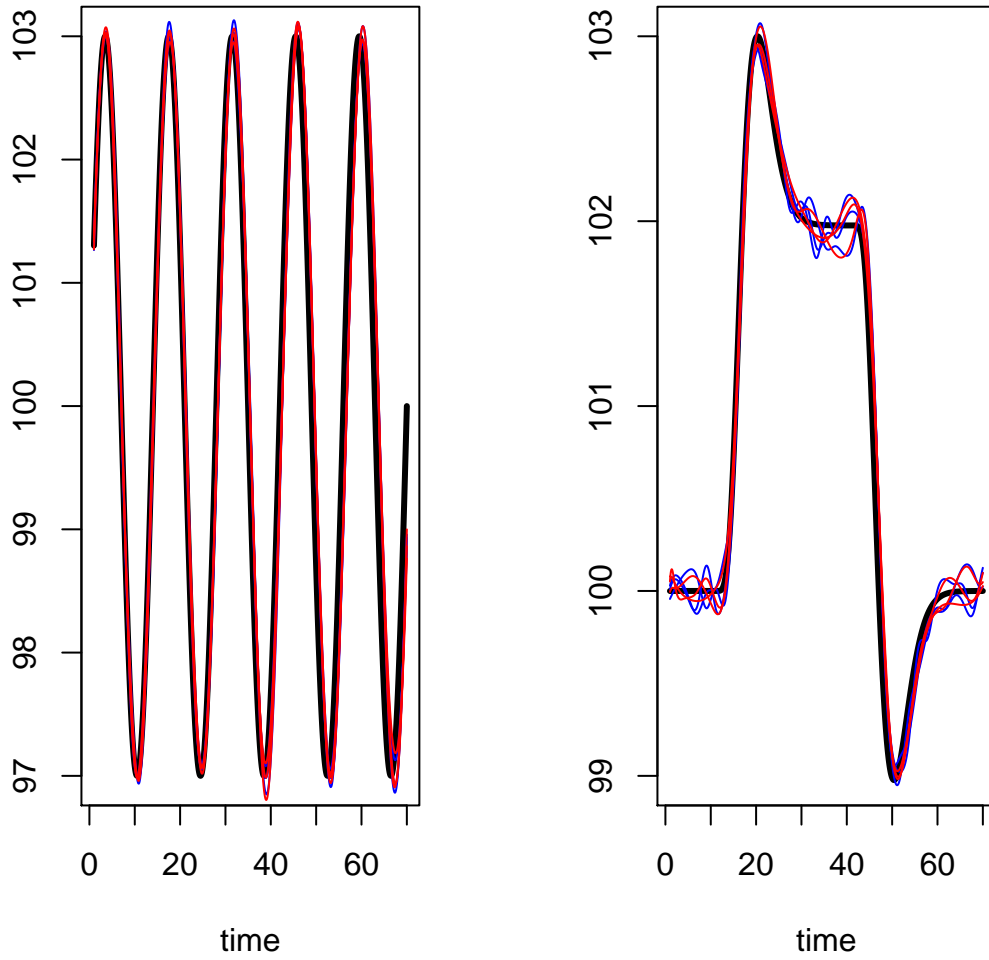


Table 1: Mean (standard deviation) of estimated correlation  $\rho = 0.4$

	$m = 5$		$m = 10$	
	L1	L2	L1	L2
<b>Sine</b>				
AIC	0.335 (0.050)	0.339 (0.054)	0.369 (0.035)	0.277 (0.163)
BIC(m)	0.332 (0.050)	0.335 (0.052)	0.369 (0.035)	0.278 (0.164)
BIC(nm)	0.354 (0.050)	0.389 (0.054)	0.375 (0.035)	0.292 (0.172)
No Penalty	0.333 (0.051)		0.369 (0.034)	
<b>fMRI</b>				
AIC	0.373 (0.035)	0.356 (0.052)	0.372 (0.035)	0.374 (0.034)
BIC(m)	0.374 (0.035)	0.348 (0.051)	0.374 (0.035)	0.377 (0.035)
BIC(nm)	0.394 (0.038)	0.413 (0.053)	0.391 (0.036)	0.404 (0.033)
No Penalty	0.333 (0.051)		0.333 (0.051)	

Table 2: Mean (standard deviation) of estimated error variance  $\sigma^2 = 1$

	$m = 5$		$m = 10$	
	L1	L2	L1	L2
<b>Sine</b>				
AIC	0.900 (0.078)	0.864 (0.088)	0.944 (0.064)	0.707 (0.415)
BIC(m)	0.891 (0.079)	0.852 (0.080)	0.946 (0.064)	0.709 (0.416)
BIC(nm)	0.951 (0.089)	0.970 (0.097)	0.964 (0.067)	0.739 (0.433)
No Penalty	0.844 (0.075)		0.929 (0.064)	
<b>fMRI</b>				
AIC	0.954 (0.065)	0.909 (0.090)	0.954 (0.065)	0.955 (0.067)
BIC(m)	0.958 (0.065)	0.889 (0.090)	0.957 (0.065)	0.963 (0.070)
BIC(nm)	1.002 (0.078)	1.022 (0.103)	0.997 (0.072)	1.017 (0.073)
No Penalty	0.844 (0.075)		0.844 (0.074)	

Table 3: Mean (standard deviation) of estimated random intercept variance  $\tau^2 = 100$

	$m = 5$		$m = 10$	
	L1	L2	L1	L2
<b>Sine</b>				
AIC	80.073 (51.595)	78.669 (51.625)	94.472 (37.883)	71.564 (51.549)
BIC(m)	80.074 (51.596)	78.670 (51.626)	94.472 (37.883)	71.563 (51.548)
BIC(nm)	80.071 (51.596)	78.662 (51.624)	94.471 (37.884)	71.562 (51.548)
No Penalty	78.671 (51.626)		94.652 (37.882)	
<b>fMRI</b>				
AIC	94.472 (37.884)	78.667 (51.624)	94.472 (37.884)	95.246 (35.224)
BIC(m)	94.471 (37.884)	78.668 (51.624)	94.471 (37.884)	95.246 (35.224)
BIC(nm)	94.469 (37.883)	78.661 (51.624)	94.469 (37.883)	95.243 (35.224)
No Penalty	78.670 (51.626)		78.673 (51.618)	

Table 4: Mean (standard deviation) of integrated square error

	$m = 5$		$m = 10$	
	L1	L2	L1	L2
<b>Sine</b>				
AIC	26.544 (5.029)	28.022 (5.500)	21.657 (3.719)	16.991 (10.299)
BIC(m)	26.593 (5.055)	27.745 (5.468)	21.675 (3.720)	17.069 (10.344)
BIC(nm)	27.948 (5.508)	32.797 (7.144)	22.567 (3.555)	18.957 (11.469)
No Penalty	27.791 (5.233)		22.566 (3.678)	
<b>fMRI</b>				
AIC	6.066 (1.588)	11.171 (2.871)	6.076 (1.606)	6.457 (2.697)
BIC(m)	6.008 (1.500)	11.239 (3.102)	6.050 (1.578)	6.599 (2.738)
BIC(nm)	7.458 (2.455)	14.791 (3.927)	7.199 (2.190)	8.672 (3.460)
No Penalty	12.479 (2.930)		12.449 (2.990)	

Figure 2: Boxplots of estimated correlation  $\rho = 0.4$ . Left panel: without random effects; right panel: with random effects. (a)  $m = 5$ , (b)  $m = 10$ , (c)  $m = 40$ .

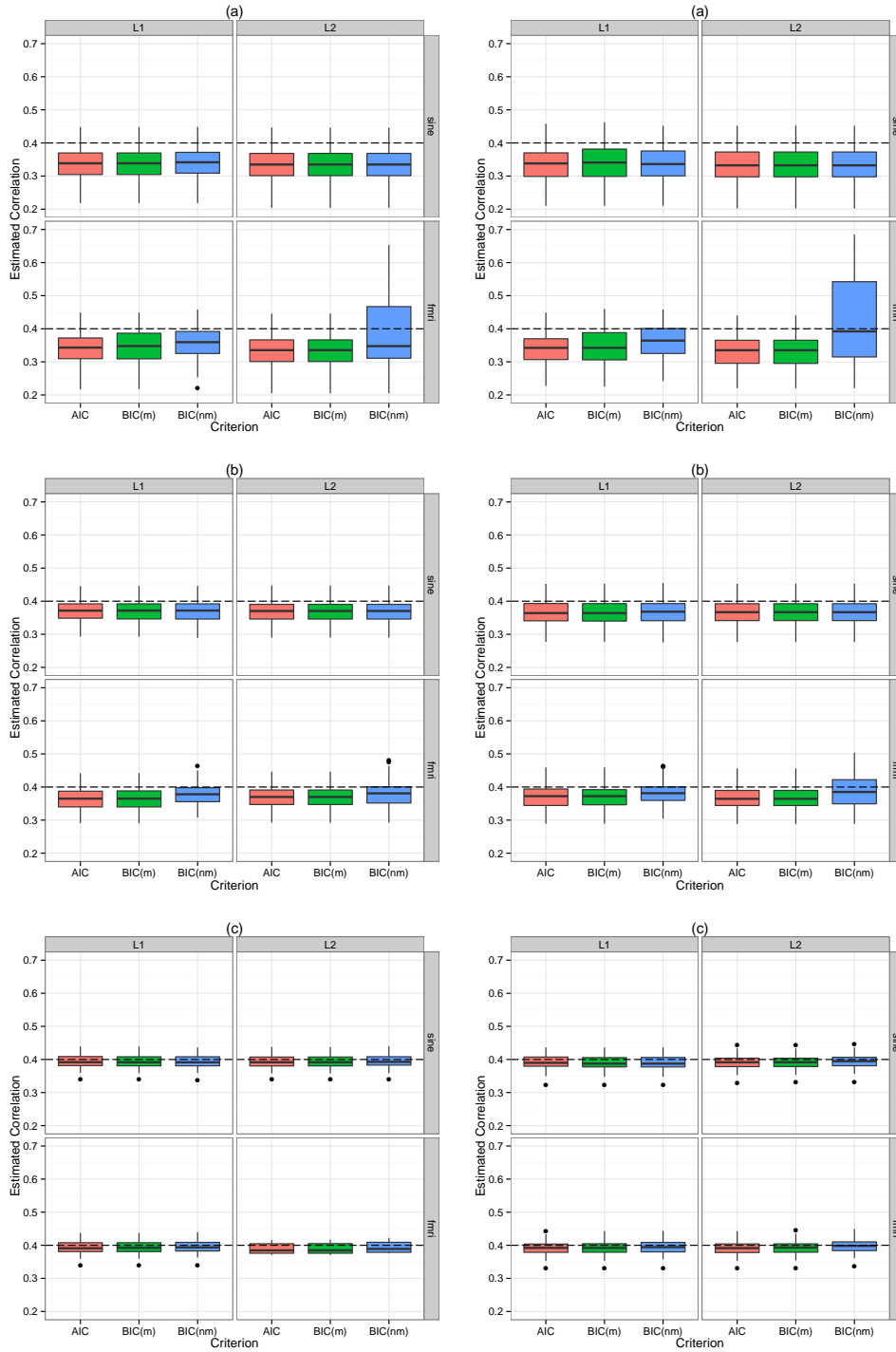


Figure 3: Boxplots of estimated error variance  $\sigma^2 = 0.09$ . Left panel: without random effects; right panel: with random effects. (a)  $m = 5$ , (b)  $m = 10$ , (c)  $m = 40$ .

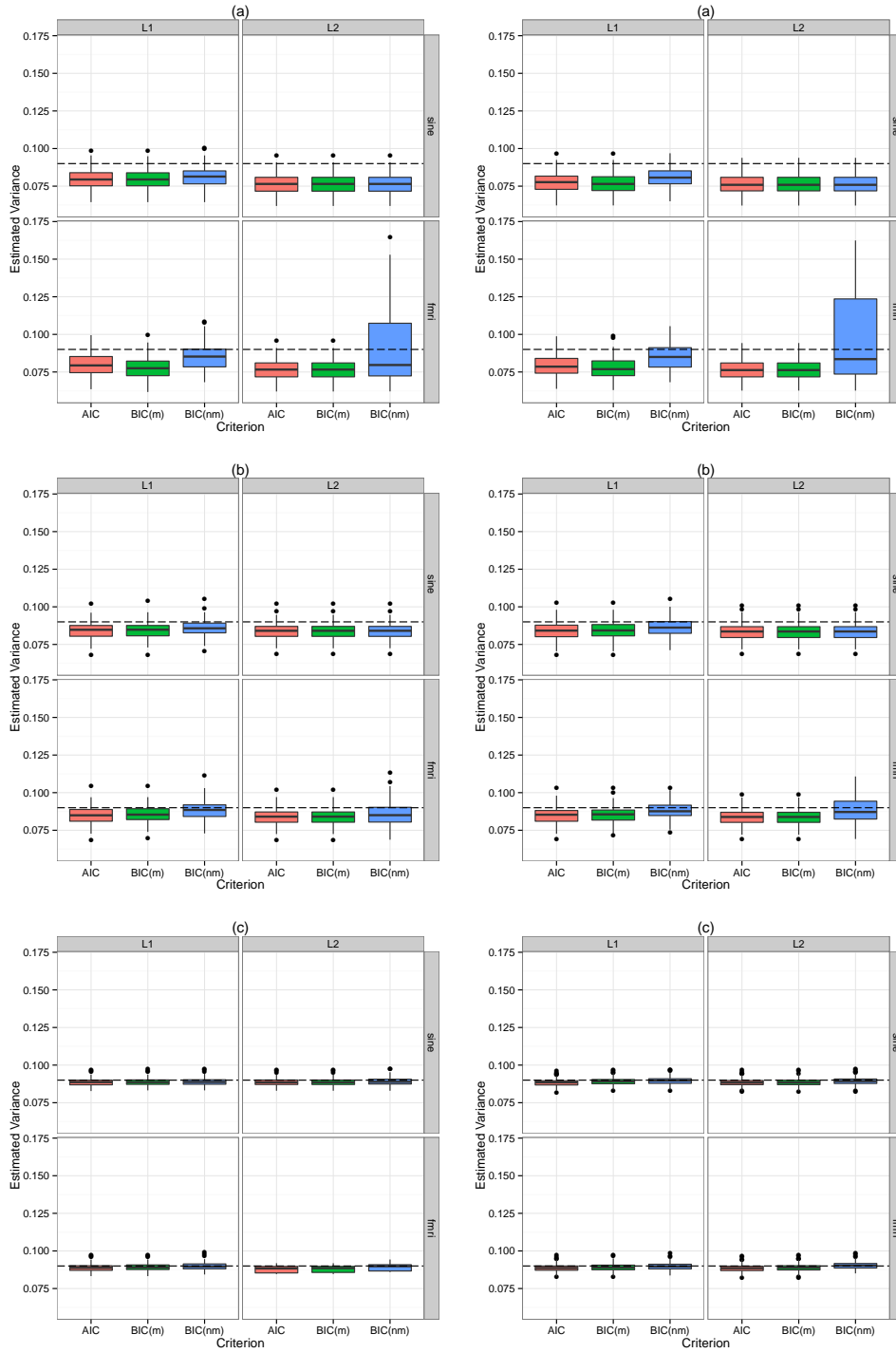




Figure 4: Boxplots of Estimated Random Intercept Variance  $\tau^2 = 100$ : (a)  $m = 5$ , (b)  $m = 10$ , (c)  $m = 40$ .

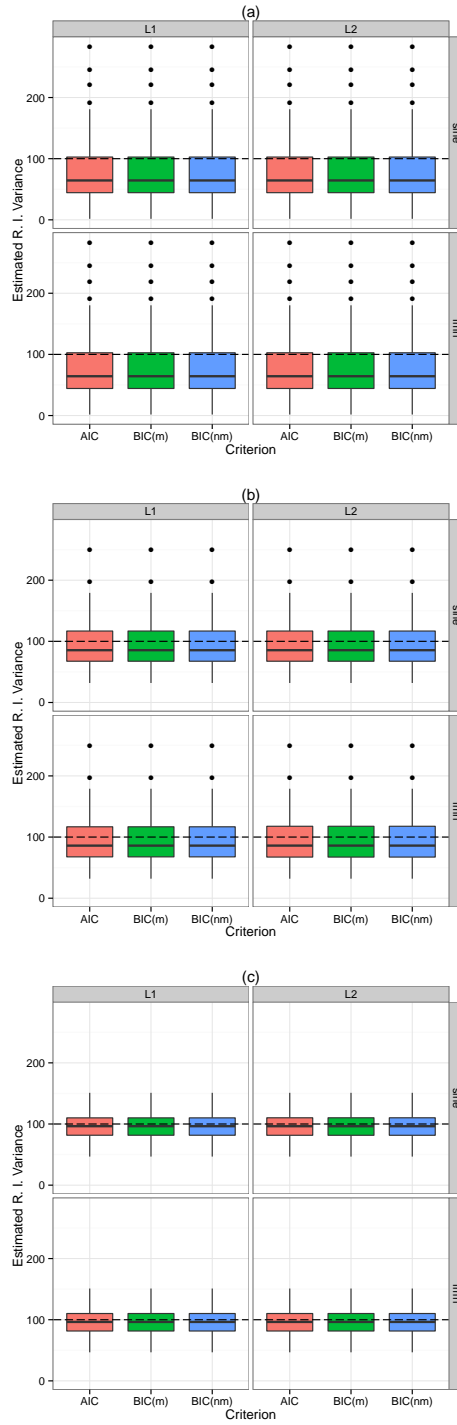


Figure 5: Boxplots of estimated correlation  $\rho = 0.4$ . (a)  $m = 5$ , (b)  $m = 10$ .

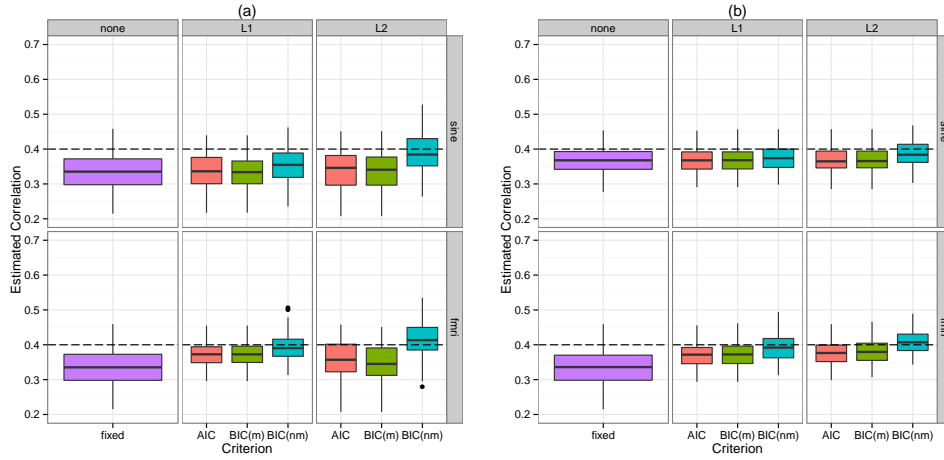


Figure 6: Boxplots of estimated error variance  $\sigma^2 = 1$ . (a)  $m = 5$ , (b)  $m = 10$ .

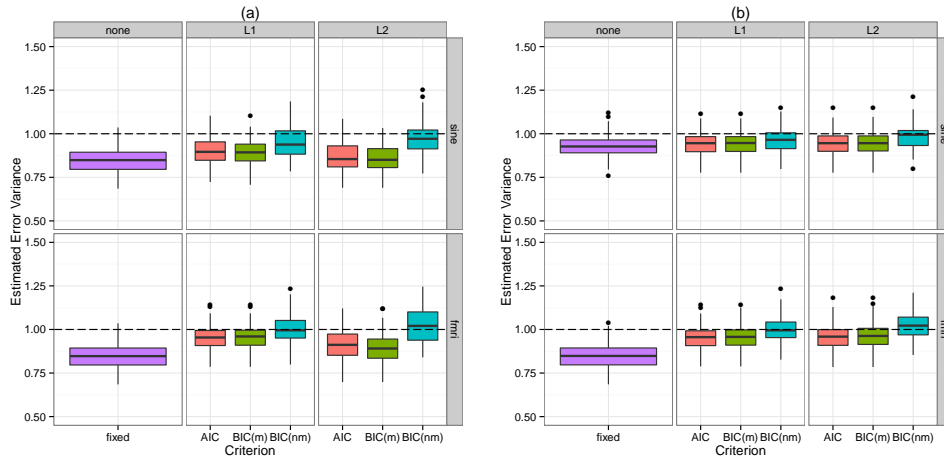


Figure 7: Boxplots of estimated random intercept variance  $\tau^2 = 100$ . (a)  $m = 5$ , (b)  $m = 10$ .

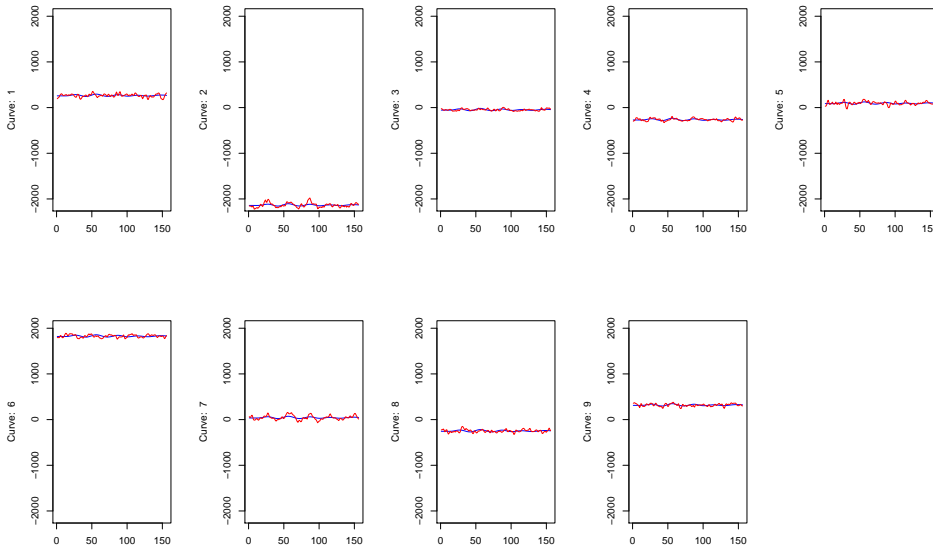
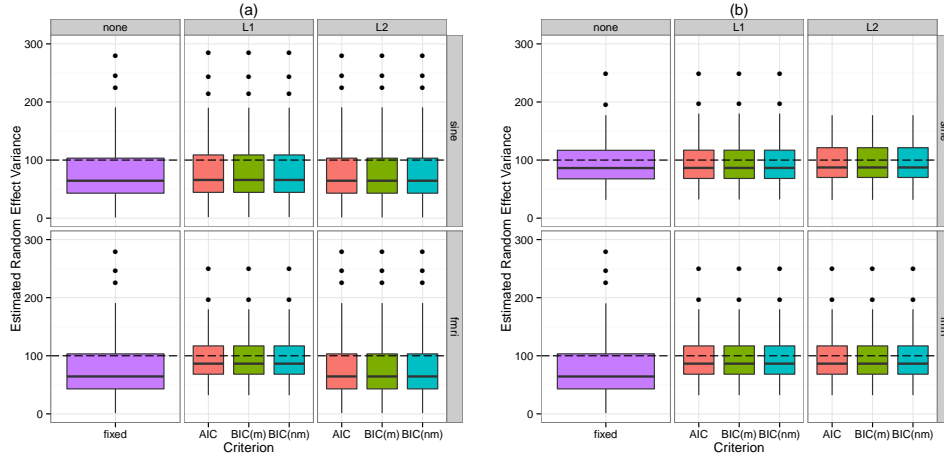


Figure 8: Voxel averaged pre - post difference for each subject: observed data (red) and  $L_1$  fitted (blue).

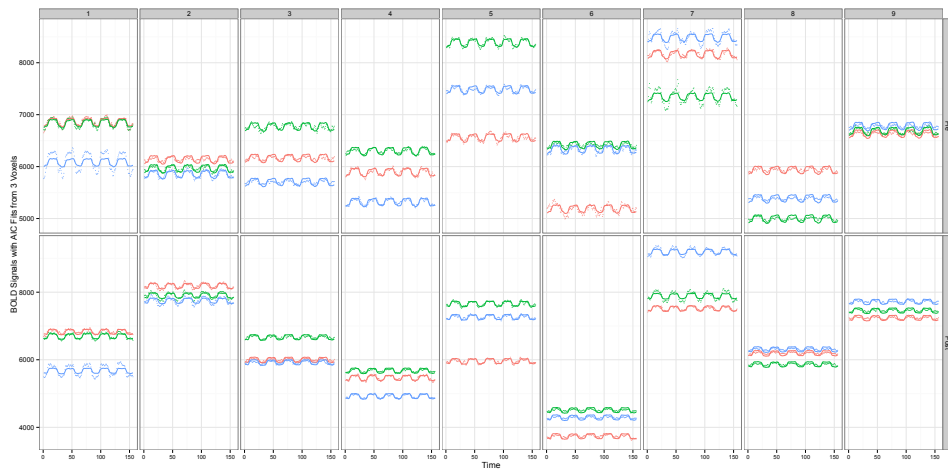


Figure 9: Three randomly selected voxels per subject and session: observed data (dots) and  $L_2$  fitted (solid).

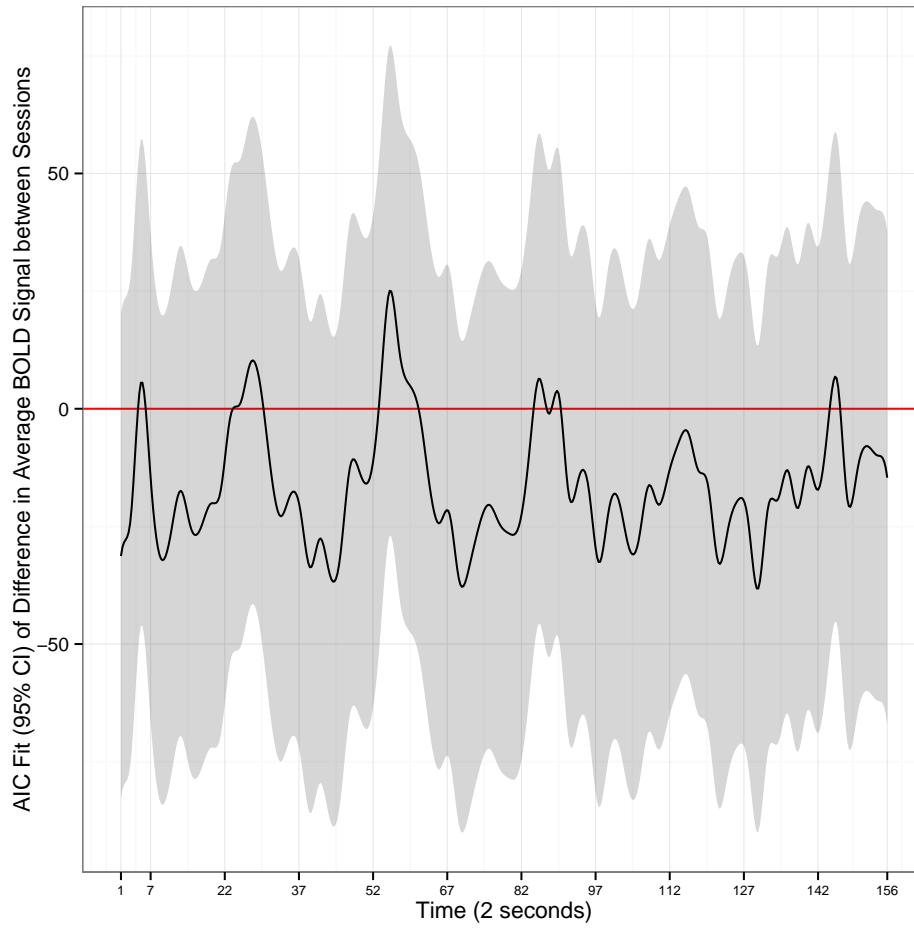


Figure 10: Estimated pre-post caffeine activation difference in BOLD signals with pointwise 95% confidence intervals (shaded).